A Cellular Automata Model for Pedestrian and Group Dynamics
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Crystals of Crowd: Modeling Pedestrian Groups Using MAS-based Approach
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Outline of Presentation

• Goal and Motivation
• State of the Art
• GA-PED model
• Crowd Crystals Model
• Conclusions and Future developments
• References
Goals and Motivations (I)

GOAL
New computational models for the representation and the simulation of the dynamical behavior of groups of pedestrians within a crowd.
Goals and Motivations (II)

• To face challenging problems in the Pedestrian Dynamics field

• To develop computer-based systems to support crowd and collective spaces management

• To test the results on real cases through experimental and calibration activities
State of the Art: Group Modeling in PED

Pedestrian Dynamics Simulation
- Force based approach
- CA-based approach
- MAS-based approach

Group modeling and cultural differences among pedestrians within a crowd are open issues in the Pedestrian Dynamics field.
State of the Art: Group Modeling in PED

First proposals exploiting traditional models:

- Holonic multiagent multilevel model [Gau07]
- Group dynamics in social force model [Mou09]
- Group dynamics in CA-based approach [Sar09]
- Groups dynamics by means of utility function and social comparison theory [Qiu10a]

Other proposals focusing on the concept of group:

- Group dynamics considering group morphology starting from observation [Mou10]
- Group dynamics by means of weighted matrices modeling inter and intra relationships [Qiu10b]
Multidisciplinary approach

“A number of things or persons being in some relation to one another”
[WikiPedia]

“An arrangement of relationships between components or individuals which produces a unit or a system”
[Ferber, 99]

“A number of individuals assembled together or having some unifying relationship”
[Webster Dictionary]

“A whole of individuals with a common goal and/or a common perceived identity”
[Social Science Encyclopedia]

Public space

Personal space

Intimate space

Social Space
Our Proposals

GA-Ped Model based on CA-approach

Crowd Crystals Model based on MAS-approach

CRYSTALS Project
GA-Ped Model

It is our first attempt to deal with the simulation of groups of pedestrians using a discrete approach.

This model is influenced by:

- Cellular Automata Models for Traffic Simulation;
- Cellular Automata Floor Field Models for Pedestrian Simulation;
- Agent-based Models for Pedestrian Simulation.
GA-Ped: Features

- Discrete space;

- It is possible to introduce groups of pedestrians with different sizes and behaviors;

- The movement of pedestrians is influenced differently by the presence of pedestrians belonging to the same group or by the presence of strangers;

- Pedestrians have a realistic perception model;

- Discrete-time dynamical system;

- Update rules are applied to all pedestrians following the *shuffled sequential update* method (necessary due to a reservation mechanism).
Mutuated from the Cellular Automata theory: the space is discretized into squared cells with fixed width (two dimensional grid);

In the primary version of the model the cell size is 40by40cm² (the typical space occupied by a pedestrian in a dense crowd);

Modeled using a three-layer structure.
GA-Ped: three Layers Structure

1. Layer 1
Details about the environment are saved into this layer (e.g. walls, obstacles, ...);

2. Layer 2
Contains information about the values of the floor field into each cell;

3. Layer 3
Stores the position of each pedestrian
Each cell can be occupied by only one pedestrian.
GA-Ped: Generating Spots

A generating spot consists in a group of cells, located in the same area, that can generate pedestrians following the same set of rules of generation, based on these parameters:

- max pedestrians
- group classes
- itineraries
- frequency of generation
- max population size

The density of the system may not be an input parameter: it is possible to determine the size of the population, but it is also possible to influence its value by determining the frequency of generation of new pedestrians in each spot.
floor fields can be thought of as a grid of cells underlying the primary grid of the environment;

- they contains information suggesting the shortest path to reach the destination;

- in our model floor fields are static;

- one floor field for each target.
GA-Ped: Pedestrian Characterization

Elementary characterization of pedestrians:

- pedID;
- Primary group;
- Schedule/itinerary.

In the future may be extended, e.g.:

- Stress index;
- Gender;
- Age;
- Ethnicity;
- ...;
GA-Ped: Pedestrian Behavior

The behavior is modeled using a Deterministic Finite Automaton
GA-Ped: Pedestrian Perception Model

The main idea for the perception model consists in the use of *perception fans*.

A *perception fan* determines how far a pedestrian can see and how he evaluates different objects according to their distance.
GA-Ped: Pedestrian Movement Evaluation

Movements are possible along eight directions (cells with Tchebychev distance = 1), it is possible to keep the current position.

We defined the likability of a movement, as influenced by:

1. goal driven component (least effort theory) (+)
2. group cohesion (+)
3. geometrical repulsion (walls, obstacles, ...) (-)
4. proxemic repulsion (-)
5. stochasticity (+)

A pedestrian will choose a movement that maximizes the likability, i.e. the benefits obtained travelling into that particular position.
GA-Ped: pedestrian movement evaluation

Observation flow, perceptive capabilities for a pedestrian walking north-east, with five dimensions, and three weight matrices for walls, pedestrian belonging to the same group and to other groups.

Sample scenario: pedestrian walking south-east, in a west-east corridor, with walls, 3 friends and 8 pedestrians belonging to other groups.

Scenario evaluation: pedestrian evaluates the floor field, the presence of walls, friends and other pedestrians according to the weights of the observation flow.

(ii) Floor field

(iii) Walls

(iv) Pedestrians, same group

(v) Pedestrians, other groups

(iv) Weight matrix for walls

(iv) Weight matrix for same group

(iv) Weight matrix for different group

(iii) Walls evaluation

(iv) Pedestrians evaluation, same group

(iv) Pedestrians evaluation, other groups
GA-Ped: pedestrian movement evaluation

1. goal driven component ($\rightarrow$ floor field value)
   \[ l_2(c_{x,y}, t) \]

2. group cohesion ($\rightarrow$ presence of other members of the same group)
   \[ \zeta(\text{group}, d, (x, y), g) = \sum_{c_{i,j} \in \zeta_{x,y,d}} w_{i,j}^\zeta \cdot l_3(c_{i,j}, g) \]

3. geometrical repulsion ($\rightarrow$ presence of obstacles)
   \[ \zeta(\text{walls}, d, (x, y)) = \sum_{c_{i,j} \in \zeta_{x,y,d}} w_{i,j}^\zeta \cdot l_1(c_{i,j}) \]

4. proxemic repulsion ($\rightarrow$ presence of strangers)
   \[ \zeta(\text{strangers}, d, (x, y), g) = \sum_{c_{i,j} \in \zeta_{x,y,d}} w_{i,j}^\zeta \cdot (1 - l_3(c_{i,j}, g)) \]

Likability formula:
\[
\begin{align*}
li(c_{x,y}, d, g, t) &= j_r \cdot \text{field}(t, (x, y)) + j_g \cdot \zeta(\text{group}, d, (x, y), g) - \\
&\quad j_w \cdot \zeta(\text{walls}, d, (x, y)) - j_n \cdot \zeta(\text{strangers}, d, (x, y), g) + \epsilon 
\end{align*}
\]
GA-Ped: implementation

• Python 2.6;
• SQLite;
• multiprocessing module (built-in);
• PIL Python Imaging Library;
Simulation: scenario

Rectangular Corridor

L-shaped corridor

Why? We have data empirically collected on these two particular configurations
Simulation: fundamental diagram

flux/density relationship
- group size: 4
- group percentage: 0.4
- #sims/frequency: 15
Flux grows until a critical density is reached. Then the flux slowly decreases and the variance increases, as the frequency of collisions increases.
Other interesting results

- lane formation at high densities;
- group dispersion tends to grow with larger groups;
- group dispersion is higher in crowded environments;
- the higher is the number and the size of the groups into the environment, the less will be the total flow, due to the higher degree of friction between different groups;
- the presence of small groups (size 2) often improves the overall flow, because they limit turbolences and conflicts around then bend, allowing the formation of relatively stable lanes (L-curve scenario);
Crowd Crystals Model

Features of the Crowd Crystals Model:

- Agent-based approach;
- Explicit representation and modeling of groups (i.e. crystals);
- Derived from sociological theories and empirical studies;
- General and platform-independent model without an explicit description of space, time, perception functions;
- Formal description of the main elements of the system;
- Behavioral functions of pedestrians inside and outside groups;
- Analysis of internal states of agents;
Definition of the Main Elements (I)

- A crowd can be seen as a set of crystals, according to the theory of Elias Canetti;
- We define a crowd as a system:
  \[ S = \langle A, G, R, O, C \rangle \]
  - \( A = \{a_1, ..., a_n\} \) is the population of agents;
  - \( G = \{G_1, ..., G_n\} \) is a finite set of groups;
  - \( R = \{r_1, ..., r_l\} \) is a finite set of static binary relationships defined on the system;
  - \( O = \{o_1, ..., o_k\} \) is a finite set of goals present in the system;
  - \( C = \{C_1, ..., C_s\} \) is a family of features defined on the system regarding the groups where each \( C_i \) is a set of possible values that the \( i^{th} \) feature can assume;
Definition of the Main Elements (II)

- Main aspects in group definition:
  - relationship among members;
  - shared goal;
- We define a crystal as:
  \[ G_i = \langle A_i, z_i, r_i, o_i \rangle \]
  - \( A_i \subseteq A \) is a finite set of agents belonging to \( G_i \);
  - \( z_i \in C_1 \times \ldots \times C_s \) is a vector with the values of features related to \( G_i \);
  - \( r_i \in R \) is a static irreflexive, symmetric relationship among agents in \( G_i \) such that for all \( a,b \in A \) with \( a \neq b \) \((a,b)\) is the transitive closure of \( r_i \);
  - \( o_i \) is the goal associated to \( G_i \);
Definition of the Main Elements (IIb)

- Considerations on the population of agents:

\[ A_i \cap A_j = \emptyset \quad \forall i, j = 1, \ldots, m \quad \text{and} \quad i \neq j \]

\[ A = \bigcup_{i=1}^{m} A_i \]

- Graph \( G_{A_i} = (A_i, E_i) \) where:
  - \( A_i \) is the set of agents belonging to \( G_{i} \);
  - \( E_i \) is the set of edges given by the relationship \( r_i \);
  - \( G_{A_i} \) is a non-oriented and connected graph;
Definition of the Main Elements (III)

- Definition of agents: every agent represents a pedestrian within a crowd;
- \( L=\{L_1, \ldots, L_q\} \) is a family of agent features where \( L_i \) is a set of possible values that the \( i^{th} \) feature can assume;
- Every agent is defined as
  \[
  a = \langle w_a \rangle
  \]
  where:
  - \( w_a \in L_1 \times \ldots \times L_q \) is a vector with the values of features related to agent \( a \);
Behavioral Rules

- Two main rules:
  - To maintain a minimum distance from pedestrians belonging to the other groups;
  - To keep a maximum distance from other agents belonging to the same group;
Distance Function

- We define a pseudo-semi-metric:
  \[ p = A \times A \mapsto D \]
  that is a function that measures distances between agents, such that, given two agents \( a, b \in A \) \( p(a, b) = p(b, a) \) and \( p(a, a) = 0_D \).

- \( D \) is a domain of distances described as a totally ordered set with \( 0_D \) as minimal element;

- We can reduce the complexity of \( D \) and admit \( D \subset \mathbb{R}^+ \).
Safe Proxemic Rule

- Every agent $a \in A$ belonging to a group $G_i$ is characterized by a personal distance $d_a \in D$:

$$d_a : \left( \prod C \right) \times \left( \prod L \right) \rightarrow D$$

- An agent $a \in G_i$ is in a safe proxemic condition iff:

$$\neg \exists b \in A \setminus A_i : p(a, b) \leq d_a$$
Safe Group Rule

- Every group $G_i$ is characterized by a private distance $\delta_{G_i} \in D$:

$$dg : \left( \prod C \right) \mapsto D$$

- We introduce a dynamic relationship $r_t$ such that $r_t$ is a dynamic irreflexive and symmetric relationship among agents in $G_i$ at a particular time $t$:

$$\forall a, b \in G_i, (a, b) \in r_t \iff p(a, b) \leq \delta_{G_i}$$

- Considering the graph structure given by $r_t$ we can define the safe group condition considering the whole history of the graph and the function:

$$\Gamma(\langle r_j | j \leq t \rangle) \in \{0,1\}$$
Internal States of Agents

SPG = Safe Proxemic and Group state;

SP = Safe Proxemic state;

SG = Safe Group state;

U = Unsafe state

Every agent is a singleton

Only one group
Case of Study: CRYSTALS Project

The main focus of CRYSTALS is to investigate how the presence of heterogeneous groups influence emergent dynamics in Hajj (pilgrimage towards Makka).
Case of Study: CRYSTALS Project

- Analysis on types of groups during Hajj:
  - Primary group;
  - Residential group;
  - Kinship group;
  - Functional group.
Modeling Groups in the Scenario of Arafat I Station

- The system can be defined as:
  - \( A = \{a_1, \ldots, a_{52}\} \);
  - \( G = \{G_1, \ldots, G_4\} \);
  - \( R = \{p, k, r, f\} \);
  - \( O = \{C\} \);
  - \( C = \{\text{country, language, social rank}\} \).

- The four groups are defined as:
  - \( G_1 = \langle A_1, (\text{Saudi Arabia, Arabic, low}), k, C \rangle \);
  - \( G_2 = \langle A_2, (\text{Saudi Arabia, Arabic, medium}), p, C \rangle \);
  - \( G_3 = \langle A_3, (\text{Saudi Arabia, Arabic, medium}), p, C \rangle \);
  - \( G_4 = \langle A_4, (\text{Saudi Arabia, Arabic, high}), p, C \rangle \);

- Family of feature \( L = \{\text{gender, age, marital status, impaired status}\} \)
  - \( a_i = \langle \text{male, adult, married, not impaired} \rangle \)
MAKKSim: Dealing with Pedestrian Groups in MAS-based Crowd Simulation (DEMO SESSION)

- Tool based on Blender;
- Provides design tools for what-if scenarios;
- Generates effective 3D visualization of crowd dynamics;
- The platform includes some aspects of Crowd Crystals Model;
- The environment processing and the management of agents movement are based on GA-Ped Model.
Conclusion and Future developments

❖ What we got:
   ❖ Original models to face the problem of representing pedestrian groups within a crowd;
   ❖ A CA-based model tested on simple scenarios, gathering results that are in tune with the existing literature;
   ❖ An agent-based abstract model to propose guidelines to include the concept of group in previous pedestrian dynamics model.

❖ Future directions:
   ❖ A deeper analysis and extensions of the notion of group and the related dynamics;
   ❖ Calibration and testing of MAKKSim and the alignment with the agent-based model.
References (some..)


• Canetti, E.: Crowds and Power. Victor Gollancz Ed. (1962)


Thank you!

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